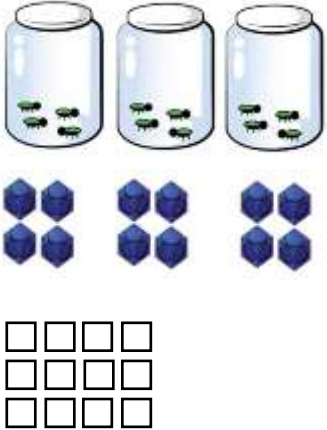


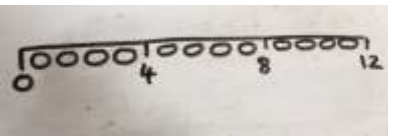



Key vocabulary: double, times, multiplied by, the product of, groups of, lots of, equal groups		
Concrete	Pictorial	Abstract
<p>Repeated grouping/repeated addition</p> <p>3×4 $4 + 4 + 4$ There are 3 equal groups, with 4 in each group.</p> 	<p>Children to represent the practical resources in a picture and use a bar model.</p>  <p>X X X X X X X X X X X X</p>	<p>$3 \times 4 = 12$</p> <p>$4 + 4 + 4 = 12$</p> <p>Children should use facts.</p>
<p>Number lines to show repeated groups- 3×4</p> 	<p>Represent this pictorially alongside a number line e.g.:</p> 	<p>Abstract number line showing three jumps of four.</p> <p>$3 \times 4 = 12$</p> 



Multiplication Routeway

Partition to multiply using base 10 or Cuisenaire rods.

$$4 \times 15 =$$

T	O
	■ ■ ■ ■ ■
	■ ■ ■ ■ ■
	■ ■ ■ ■ ■
	■ ■ ■ ■ ■

$$40 + 20 = 60$$

Children to represent the concrete manipulatives pictorially.

$$4 \times 15 =$$

T	O
	x x x x x
	x x x x x
	x x x x x
	x x x x x

$$40 + 20 = 60$$

Children to be encouraged to show the steps they have taken.

$$4 \times 15$$

$$4 \times 5 = 20$$

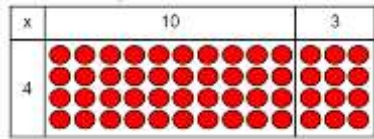
$$4 \times 10 = 40$$

$$20 + 40 = 60$$

Multiplication Routeway

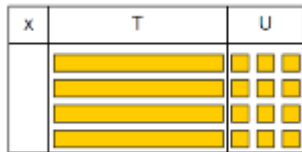
Grid Method

Show the link with arrays to first introduce the grid method.



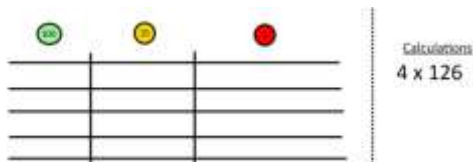
4 rows of 10
4 rows of 3

Move on to using Base 10 to move towards a more compact method.

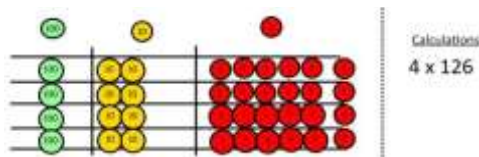


4 rows of 13

Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.



Fill each row with 126.



Add up each column, starting with the ones making any exchanges needed.

Children can represent the work they have done with place value counters in a way that they understand. They can draw the counters, using numbers to show different amounts or just use circles in the different columns to show their thinking as shown below.

$$24 \times 3 =$$



$$60 + 12 = 72$$

Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

X	30	5
7	210	35

$$210 + 35 = 245$$

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

	10	8
10	100	80
3	30	24

X	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

Multiplication Routeway

<p>Then you have your answer.</p>														
<p>Formal column method with place value counters (base 10 can also be used.)</p> <p>3×23</p> <table border="1" style="width: 100px; text-align: center;"> <thead> <tr style="background-color: #f8d7da;"> <th>10s</th> <th>1s</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> </tbody> </table> <p>60 + 9</p>	10s	1s			<p>Children to represent the counters pictorially.</p> <p style="text-align: center;">60 + 9</p>	<p>Children to record what it is they are doing to show understanding.</p> $3 \times 23 \quad 3 \times 20 = 60$ $20 \quad 3 \quad 3 \times 3 = 9$ $60 + 9 = 69$ $\begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$								
10s	1s													
<p>Formal column method with place value counters.</p> <p>$6 \times 23 =$</p> <table border="1" style="width: 100px; text-align: center;"> <thead> <tr style="background-color: #f8d7da;"> <th>100s</th> <th>10s</th> <th>1s</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> </tr> </tbody> </table> <table border="1" style="width: 100px; text-align: center;"> <thead> <tr style="background-color: #f8d7da;"> <th>100s</th> <th>10s</th> <th>1s</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> </tr> </tbody> </table> <p>100 + 30 + 8</p>	100s	10s	1s				100s	10s	1s				<p>Children to represent the counters/base 10, pictorially e.g. the image below.</p> <p>$6 \times 23 =$</p> <p style="text-align: center;">100 + 30 + 8</p>	<p>Expanded method</p> <p>(If it helps, children can write out what they are solving next to their answer.)</p> $\begin{array}{r} 32 \\ \times 24 \\ \hline 8 \quad (4 \times 2) \\ 120 \quad (4 \times 30) \\ 40 \quad (20 \times 2) \\ 600 \quad (20 \times 30) \\ \hline 768 \end{array}$
100s	10s	1s												
100s	10s	1s												



Multiplication Routeway

		<p>Formal written method.</p> $\begin{array}{r} 6 \times 23 = \\ 23 \\ \times 6 \\ \hline 138 \\ 11 \end{array}$ $\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2480 \\ \hline 3224 \\ 11 \end{array}$ <p>Answer: 3224</p>
<p>When children start to multiply HTO \times HTO and ThHTO \times TO etc, they should be confident with the abstract:</p>		